

# **LINEAR DIGITAL IC APPLICATIONS (LDIC)**

## **UNIT – I**

An integrated circuit (IC), sometimes called a chip or wafer on which thousands or millions of tiny resistors, capacitors are fabricated. An IC can function as a timer, counter, computer or microprocessor. A particular IC is categorized as either linear or digital depending on its intended application. A linear integrated circuit (linear IC) is a solid-state device characterized by a theoretically infinite number of possible operating states. It operates over a continuous range of input levels. In contrast, an IC has a finite number of discrete input and output states. Digital IC is expressed as a series of the digits 0 and 1, typically represented by values of a physical quantity such as voltage or magnetic polarization.

### **OPERATIONAL AMPLIFIER:**

An operational amplifier is a direct coupled high gain amplifier consisting of one or more differential (OP-AMP) amplifiers and followed by a level translator and an output stage. An operational amplifier is available as a single integrated circuit package.

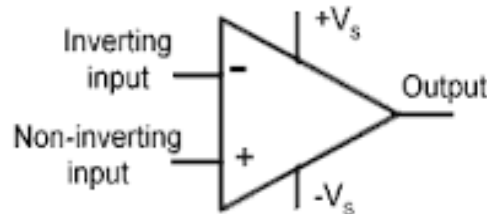


Fig 1.1 Op amp symbol

### **BLOCK DIAGRAM OF TYPICAL OP-AMP WITH VARIOUS STAGES:**

The input stage is a dual input balanced output differential amplifier. This stage provides most of the voltage gain of the amplifier and also establishes the input resistance of the OPAMP. The intermediate stage of OPAMP is another differential amplifier which is driven by the output of the first stage. This is usually dual input unbalanced output. Because direct coupling is used, the dc voltage level at the output of intermediate stage is well above ground potential. Therefore level shifting circuit is used to shift the dc level at the output downward to zero with respect to ground. The output stage is generally a push pull complementary amplifier. The output stage increases the output voltage swing and raises the current supplying capability of the OPAMP. It also provides low output resistance.

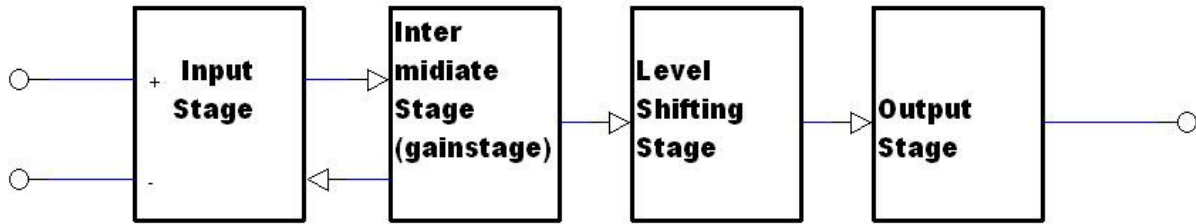


Fig 1.2 Block diagram of Op amp

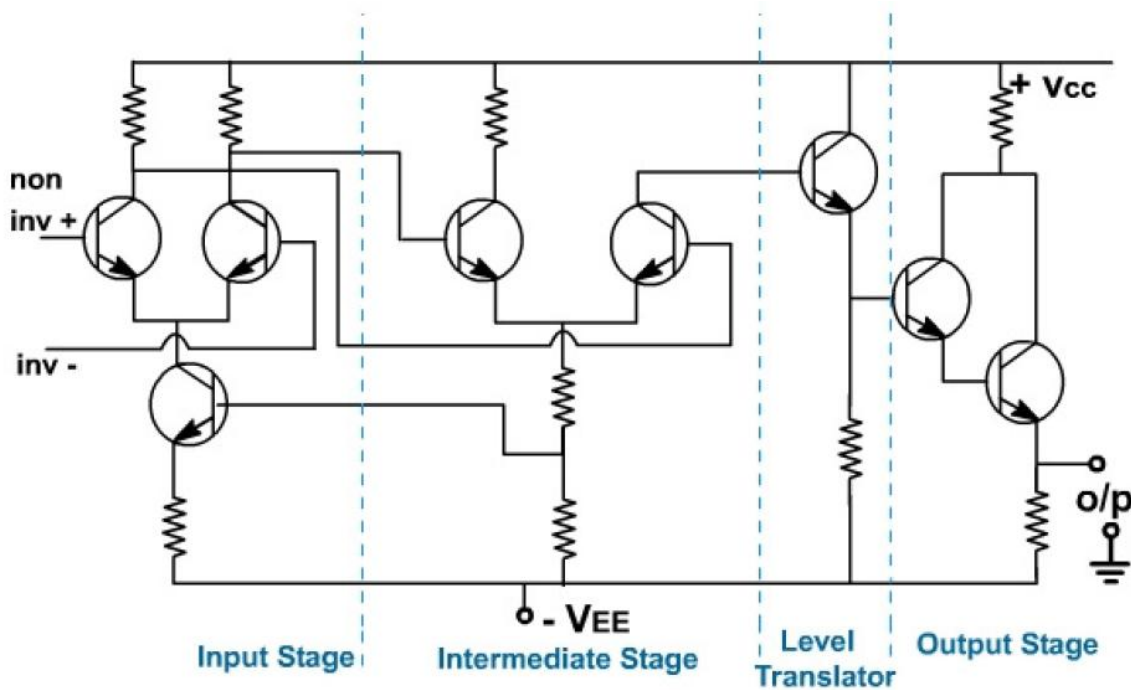


Fig 1.3 Circuit diagram of Op amp

## **DIFFERENTIAL AMPLIFIER:**

A differential amplifier is an important building block of an op amp. It is a type of electronic amplifier that amplifies the difference between two input voltages but suppresses any voltage common to the two inputs. It is an analog circuit with two inputs and one output in which the output is ideally proportional to the difference between the two voltages.

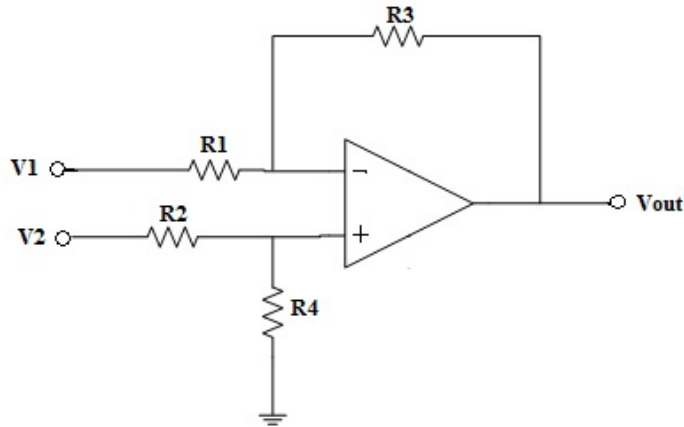


Fig 1.4 Differential amplifier circuit

There are four different types of configuration in differential amplifier which are as follows:

- i) Dual input balanced output
- ii) Dual input unbalanced output
- iii) Single input balanced output
- iv) Single input unbalanced output

### 1) DUAL INPUT, BALANCED OUTPUT DIFFERENTIAL AMPLIFIER

The circuit shown below is a dual-input balanced-output differential amplifier. Here in this circuit, the two input signals (dual input),  $V_{in1}$  and  $V_{in2}$ , are applied to the bases  $B_1$  and  $B_2$  of transistors  $Q_1$  and  $Q_2$ . The output  $V_o$  is measured between the two collectors  $C_1$  and  $C_2$  which are at the same dc potential. Because of the equal dc potential at the two collectors with respect to ground, the output is referred as a balanced output.

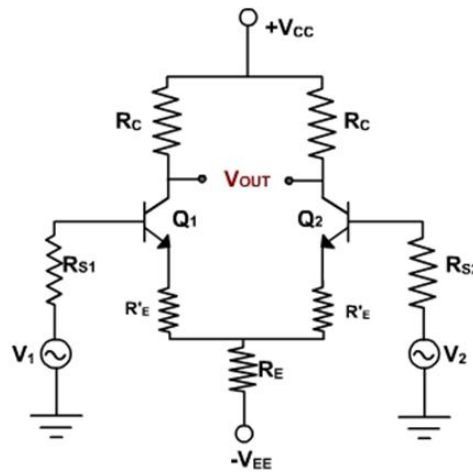


Fig 1.5 dual-input balanced-output differential amplifier circuit

## Differential Amplifier with $R_E$ DC Analysis:-

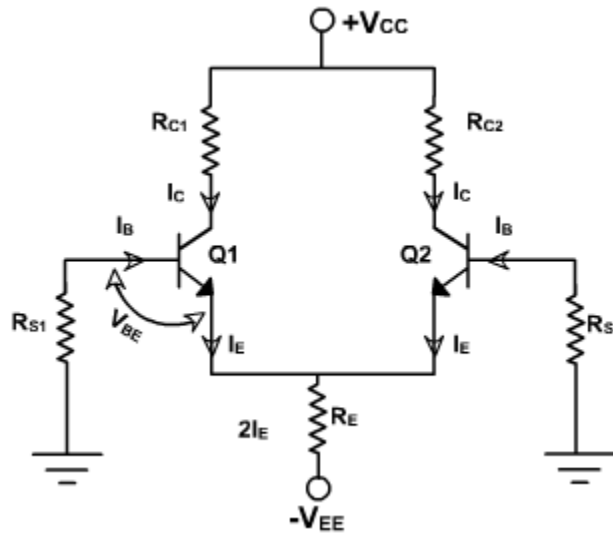


Fig 1.6 DC Equivalent Circuit For Dual-Input Balanced Output Differential Amplifier

To determine the operating point values ( $I_{CQ}$  and  $V_{CEQ}$ ) for the differential amplifier, we need to obtain a dc equivalent circuit. The dc equivalent circuit can be obtained simply by reducing the input signals  $v_{in1}$  and  $v_{in2}$  to zero. The dc equivalent circuit thus obtained is shown in fig below. Note that the internal resistances of the input signals are denoted by  $R_{in}$  because  $R_{in1} = R_{in2}$ . Since both emitter biased sections of the differential amplifier are symmetrical (matched in all respects), we need to determine the operating point collector current  $I_{CQ}$  and collector to emitter voltage  $V_{CEQ}$  for only one section. We shall determine the  $I_{CQ}$  and  $V_{CEQ}$  values for transistor  $Q_1$  only. These  $I_{CQ}$  and  $V_{CEQ}$  values can then be used for transistor  $Q_2$  also.

Applying Kirchoff's voltage law to the base-emitter loop of the transistor  $Q_1$ ,

$$R_{in} I_B - V_{BE} - R_E(2I_E) + V_{EE} = 0 \quad (1)$$

But,  $I_B = I_E/\beta_{dc}$  since  $I_C = I_E$ . Thus the emitter current through  $Q_1$  is determined directly from eqn (1) as follows :

$$I_E = (V_{EE} - V_{BE}) / (2R_E + R_{in}/\beta_{dc}) \quad (2)$$

where  $V_{BE} = 0.6V$  for silicon transistors

$V_{BE} = 0.2V$  for germanium transistors

Generally,  $R_{in}/\beta_{dc} \ll 2R_E$ . Therefore, eqn(2) can be rewritten as

$$I_{CQ} = I_E = (V_{EE} - V_{BE}) / 2R_E \quad (3)$$

From eqn(3), the value of  $R_E$  sets up the emitter current in transistors  $Q_1$  and  $Q_2$  for a given value of  $V_{EE}$ .

In other words, by selecting a proper value of  $R_E$ , a desired value of emitter current for a known value of

$-V_{EE}$  will be obtained. Notice that the emitter current in transistors  $Q_1$  and  $Q_2$  is independent of collector resistance  $R_C$ . Next we shall determine the collector to emitter voltage  $V_{CE}$ . The voltage at the emitter of transistor  $Q_1$  is approximately equal to  $V_{BE}$  if we assume the voltage drop across  $R_{in}$  to be negligible.

Knowing the value of emitter current  $I_E (=I_C)$ , we can obtain the voltage at the collector  $V_{CC}$  as follows:

$$V_C = V_{CC} - R_C I_C. \text{ Thus the collector to emitter voltage } V_{CE} \text{ is } V_{CE} = V_C - V_E = (V_{CC} - R_C I_C) - (-V_{EE})$$

$$V_{CEQ} = V_{CE} = V_{CC} + V_{BE} - R_C I_C \quad (4)$$

Thus for both transistors we can determine the operating point values by using the eqns (2) and (4), respectively, because at the operating point  $I_E = I_{CQ}$  and  $V_{CEQ} = V_{CE}$ . Remember that the dc analysis eqns (2) and (4) are applicable for all 4 differential amplifier configurations as long as we use the same biasing arrangement for each of them.

### AC Analysis with r parameters :-

To perform ac analyses to derive the expression for the voltage gain  $A_d$  and input resistance  $R_i$  of a differential amplifier:

- 1) Set the dc voltages  $+V_{CC}$  and  $-V_{EE}$  at 0
- 2) Substitute the small signal T equivalent models for the transistors

Figure below shows resulting ac equivalent circuit of the dual input balanced output differential amplifier

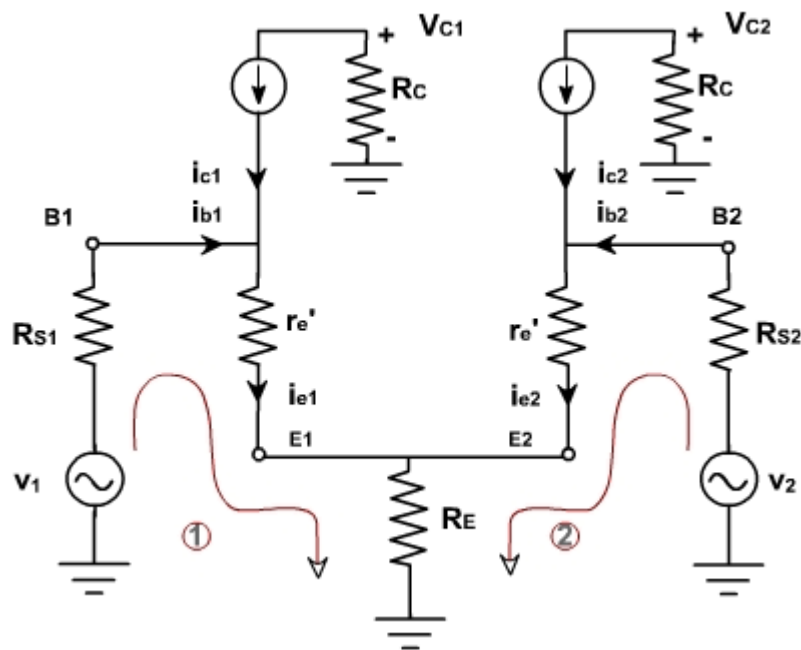


Fig 1.7 AC Equivalent circuit For Dual-Input Balanced Output Differential Amplifier

### Voltage Gain:-

Before we proceed to derive the expression for the voltage gain  $A_d$  the following should be noted about the circuit in the figure above

- 1)  $I_{e1}=I_{e2}$ ; therefore  $r_{e1}=r_{e2}$ . For this reason the ac emitter resistance of transistors  $Q_1$  and  $Q_2$  is simply denoted by  $r_e$ .
- 2) The voltage across each collector resistor is shown out of phase by  $180^\circ$  w.r.t the input voltages  $v_{in1}$  and  $v_{in2}$ .

Writing Kirchhoff's voltage equations for loops 1 and 2 gives us

$$v_{in1} - R_{in1}i_{b1} - r_e i_{e1} - R_E(i_{e1}+i_{e2}) = 0 \quad (5)$$

$$v_{in2} - R_{in2}i_{e2} - r_e i_{e2} - R_E(i_{e1}+i_{e2}) = 0 \quad (6)$$

Substituting current relations  $i_{b1} = i_{e1}/B_{ac}$  and  $i_{b2} = i_{e2}/B_{ac}$  yields

$$v_{in1} - R_{in1}i_{e1}/B_{ac} - r_e i_{e1} - R_E(i_{e1}+i_{e2}) = 0$$

$$v_{in2} - R_{in2}i_{e2}/B_{ac} - r_e i_{e2} - R_E(i_{e1}+i_{e2}) = 0$$

Generally,  $R_{in1}/B_{ac}$  and  $R_{in2}/B_{ac}$  values are very small therefore we shall neglect them here for simplicity and rearrange these equations as follows:

$$(r_e+R_E)i_{e1} + R_E i_{e2} = v_{in1} \quad (7)$$

$$R_E i_{e1} + (r_e+R_E)i_{e2} = v_{in2} \quad (8)$$

Eqns (7) and (8) can be solved simultaneously for  $i_{e1}$  and  $i_{e2}$  by using Cramer's rule:

$$I_{e1} = \frac{(v_{in1}/v_{in2})(R_E/r_e+R_E)/\{(r_e+R_E)/R_E\} \{R_E/(r_e+R_E)\}}{\{(r_e+R_E)v_{in1} - R_E v_{in2}\}/\{(r_e+R_E)^2 - (R_E)^2\}} \quad (9a)$$

Similarly

$$I_{e2} = \frac{(v_{in1}/v_{in2})\{(r_e+R_E)/R_E\}/\{(r_e+R_E)/R_E\} \{R_E/(r_e+R_E)\}}{\{(r_e+R_E)v_{in2} - R_E v_{in1}\}/\{(r_e+R_E)^2 - (R_E)^2\}} \quad (9b)$$

The output voltage is  $v_o = v_{c2} - v_{c1}$

$$\begin{aligned} &= -R_C i_{c2} - (-R_C i_{c1}) \\ &= R_C i_{c1} - R_C i_{c2} \\ &= R_C(i_{e1} - i_{e2}) \quad \text{since } i_c = i_e \end{aligned} \quad (10)$$

Substituting current relations  $i_{e1}$  and  $i_{e2}$  in eqn(10), we get

$$\begin{aligned} v_o &= R_C \left[ \frac{(r_e+R_E)v_{in1} - R_E v_{in2}}{\{(r_e+R_E)^2 - (R_E)^2\}} - \frac{(r_e+R_E)v_{in2} - R_E v_{in1}}{\{(r_e+R_E)^2 - (R_E)^2\}} \right] \\ &= R_C \left[ \frac{(r_e+R_E)(v_{in1} - v_{in2}) + (R_E)(v_{in1} - v_{in2})}{\{(r_e+R_E)^2 - (R_E)^2\}} \right] \\ &= R_C \frac{(r_e+2R_E)(v_{in1} - v_{in2})}{r_e(r_e+2R_E)} \\ &= (R_C/r_e)(v_{in1} - v_{in2}) \end{aligned} \quad (11)$$

Thus, a differential amplifier amplifies the difference between two input signals as expected, the figure below shows the input and output waveforms of the dual-input balanced-output differential

amplifier. By defining  $v_{id} = v_{in1}$  as the difference in input voltages, we can write the voltage-gain equation of the dual-input balanced-output differential amplifier as follows:

$$\mathbf{A_d = v_o/v_{id} = RC/r_e} \quad (12)$$

### Differential Input Resistance:-

Differential input resistance is defined as the equivalent resistance that would be measured at either input terminal with the other terminal grounded.

$$\begin{aligned} R_{i1} &= |v_{in1}/i_{b1}|_{v_{in2}=0} \\ &= |v_{in1}/(i_e/\beta_{ac})|_{v_{in2}=0} \end{aligned}$$

Substituting the value of  $i_{e1}$  from eqn(9a), we get

$$\begin{aligned} R_{i1} &= \beta_{ac} v_{in1} / [\{(r_e + R_E)v_{in1} - R_E(0)\} / \{(r_e + R_E)^2 - (R_E)^2\}] \\ &= [\beta_{ac}(r_e^2 + 2r_e R_E)] / (r_e + R_E) \\ &= [\beta_{ac} r_e (r_e + 2R_E)] / (r_e + R_E) \end{aligned} \quad (13)$$

Generally,  $R_E \gg r_e$ , which implies that  $(r_e + 2R_E) = 2R_E$  and  $(r_e + R_E) = R_E$ . Therefore eqn(13) can be rewritten as  $R_{i1} = \beta_{ac} r_e (2R_E) / R_E = 2\beta_{ac} r_e$  (14)

Similarly, the input resistance  $R_{i2}$  seen from the input signal source  $v_{in2}$  is defined as

$$\begin{aligned} R_{i2} &= |v_{in2}/i_{b2}|_{v_{in1}=0} \\ &= |v_{in2}/(i_e/\beta_{ac})|_{v_{in1}=0} \end{aligned}$$

Substituting the value of  $i_{e2}$  from eqn(9b), we get

$$\begin{aligned} R_{i2} &= \beta_{ac} v_{in2} / [\{(r_e + R_E)v_{in2} - R_E(0)\} / \{(r_e + R_E)^2 - (R_E)^2\}] \\ &= [\beta_{ac}(r_e^2 + 2r_e R_E)] / (r_e + R_E) \\ &= [\beta_{ac} r_e (r_e + 2R_E)] / (r_e + R_E) \end{aligned} \quad (15)$$

However,  $(r_e + 2R_E)$  and  $(r_e + R_E) = R_E$  if  $R_E \gg r_e$ . Therefore eqn(15) can be rewritten as

$$\mathbf{R_{i2} = \beta_{ac} r_e (2R_E) / R_E = 2\beta_{ac} r_e} \quad (16)$$

### Output Resistance:-

Output resistance is defined as the equivalent resistance that would be measured at either output terminal w.r.t ground.

$$\mathbf{R_{o1} = R_{o2} = RC} \quad (17)$$

The current gain of the differential amplifier is undefined; therefore, the current-gain equation will not be derived for any of the four differential amplifier configurations.

## **2) DUAL INPUT, UNBALANCED OUTPUT DIFFERENTIAL AMPLIFIER:**

In this case, two input signals are given however the output is measured at only one of the two collector w.r.t. ground as shown in fig. 1. The output is referred to as an unbalanced output because the collector at which the output voltage is measured is at some finite dc potential with respect to ground. In other words, there is some dc voltage at the output terminal without any input signal applied. DC analysis is exactly same as that of first case.

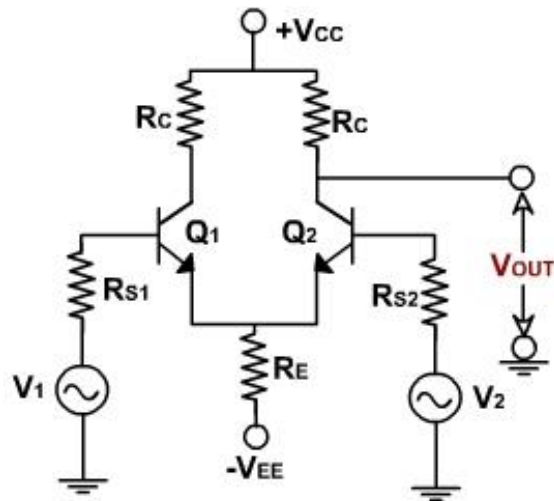


Fig 1.8 dual-input unbalanced-output differential amplifier circuit

### **DC Analysis:**

The dc analysis procedure for the dual input unbalanced output is identical to that dual input balanced output because both configuration use the same biasing arrangement. Therefore the emitter current and emitter to collector voltage for the dual input unbalanced output differential amplifier are determined from equations.

$$I_E = I_{CQ} = (V_{EE} - V_{BE}) / (2R_E + \beta_{dc})$$

$$V_{CE} = V_{CEQ} = V_{CC} - V_{BE} - R_C I_{CQ}$$

### **AC Analysis:**

The output voltage gain in this case is given by



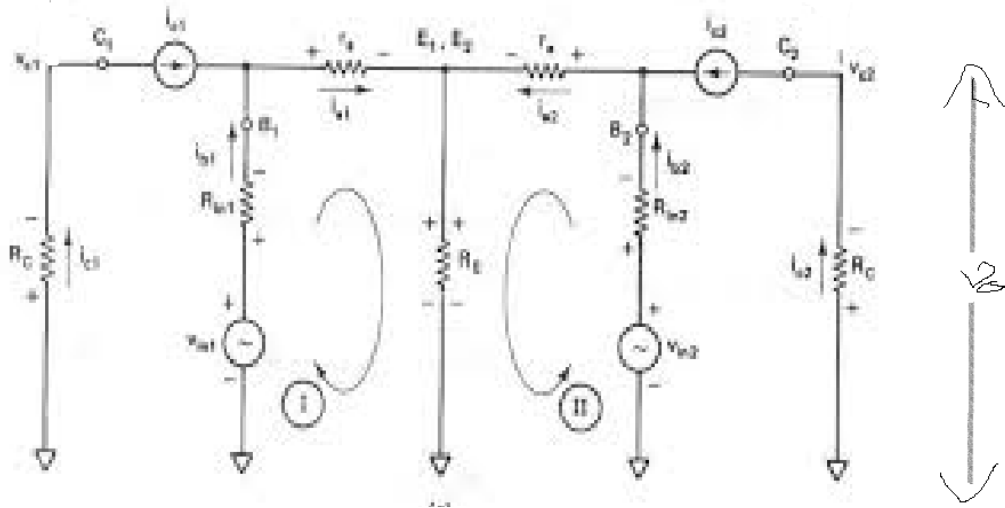


Fig 1.9 AC Equivalent circuit For Dual-Input Un-Balanced Output Differential Amplifier

### Voltage Gain:

Writing Kirchhoff's voltage equations of loops I and II is given as

$$V_{in1} - R_{in1} i_{b1} - r_e i_{e1} - R_E (i_{e1} + i_{e2}) = 0$$

$$V_{in2} - R_{in2} i_{b2} - r_e i_{e2} - R_E (i_{e1} + i_{e2}) = 0$$

Since these equations are the same as equations the expressions for  $i_{e1}$  and  $i_{e2}$  will be the same equations respectively.

$$i_{e1} = ((r_e + R_E) v_{in1} - R_E v_{in2}) / ((r_e + R_E)^2 - R_E^2)$$

$$i_{e2} = ((r_e + R_E) v_{in2} - R_E v_{in1}) / ((r_e + R_E)^2 - R_E^2)$$

The output voltage is

$$V_o = v_{c2} = -R_C i_{e2} = -R_C i_{e1} \quad \text{since } i_{c1} = i_{e2}$$

Substituting the value of  $i_{e2}$

$$V_o = -R_C ((r_e + R_E) v_{in1} - R_E v_{in2}) / ((r_e + R_E)^2 - R_E^2)$$

$$= R_C ((R_E v_{in2} - r_e + R_E) v_{in1}) / ((r_e + R_E)^2 - R_E^2)$$

Generally  $R_E \gg r_e$  hence  $(r_e + R_E) = R_E$  &  $(r_e + R_E)^2 - R_E^2 = 2R_E r_e$  Therefore

$$V_o = R_C (R_E v_{in1} - R_E v_{in2}) / (2r_e R_E)$$

$$= R_C (R_E (v_{in1} - v_{in2})) / (2r_e R_E)$$

$$= R_C (v_{in1} - v_{in2}) / (2r_e)$$

$$A_d = v_o / v_{id} = R_C / 2R_E$$

The voltage gain is half the gain of the dual input, balanced output differential amplifier. Since at the output there is a dc error voltage, therefore, to reduce the voltage to zero, this configuration is normally followed by a level translator circuit.

**Input Resistance:**

The only difference between the circuits is the way output voltage is measured. The input resistance seen from either input source does not depend on the way the output voltage is measured.

$$R_{i1}=R_{i2}=2\beta_{ac}r_e$$

**Output Resistance:**

The output resistance  $R_0$  measured at collector  $C_2$  with respect to ground is equal to the collector resistor  $R_C$ .

$$R_0=R_C$$

**3) SINGLE INPUT, BALANCED OUTPUT DIFFERENTIAL AMPLIFIER:**

Figure illustrates a differential amplifier where the input to  $Q_2$  is grounded and the output is taken as  $v_{o1}$ . As discussed in the previous section, a constant current source is used in place of  $R_{EE}$ . This configuration is known as a **single-ended input and output amplifier with phase reversal**. To analyze this amplifier, all we have to do is set  $v_2=0$  in the earlier equations. If we assume that the equivalent resistance of the current source is very large, the common-mode gain is approximately equal to zero. This means the single-ended differential-mode gain of the amplifier will determine the output, which will be

$$V_{out} = A_d V_{di} = \frac{-R_C V_1}{2r_e}$$

The negative sign indicates that there is a  $180^\circ$  phase shift between the input ( $v_1$ ) and the output ( $v_{o1}$ ).

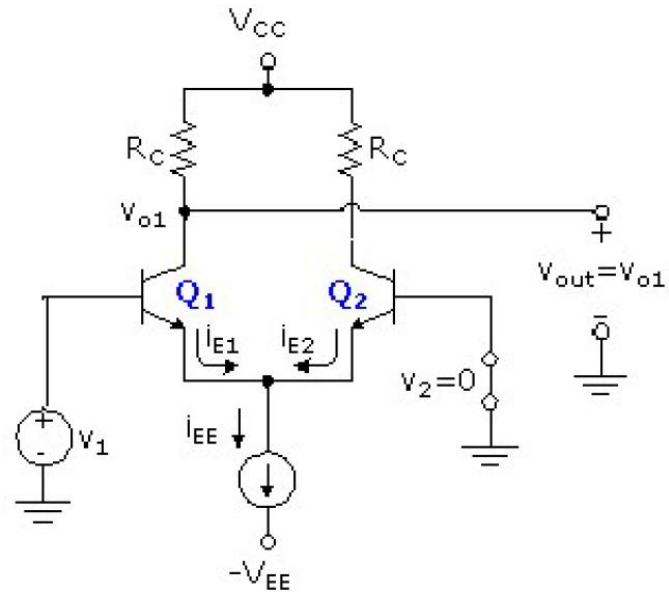


Fig 1.10 Single input and output differential amplifier

## CONSTANT CURRENT SOURCE

In the differential amplifiers discussed so far the combination of  $R_E$  and  $V_{EE}$  is used to step up the dc emitter current. We can also use constant current bias circuit to set up the dc emitter current if desired. In fact, the constant bias current circuit is better because it provides current stabilization and in turn assures a stable operating point for the differential amplifier.

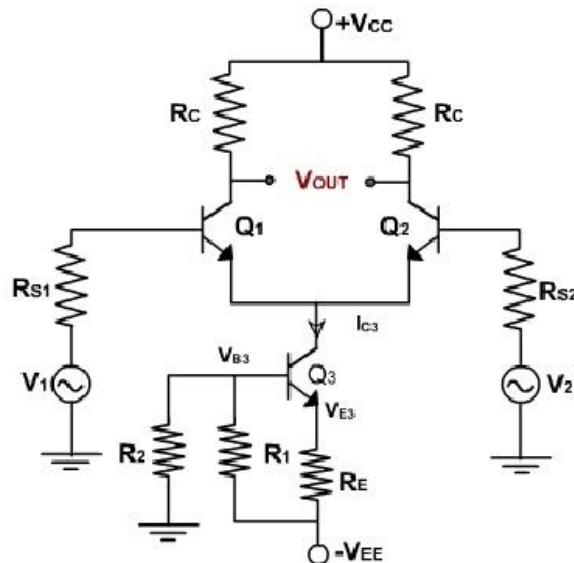


Fig 1.11 Constant Current Source

The figure shows the dual input, balanced-output differential amplifier using a resistive constant current bias. Note that the resistor  $R_E$  is replaced by a constant current transistor  $Q_3$  circuit. The dc

collector current in transistor Q<sub>3</sub> is established by resistors R<sub>1</sub>, R<sub>2</sub> and R<sub>3</sub> and can be determined as follows. Applying the voltage-divider rule, the voltage at the base of transistor Q<sub>3</sub> is

$$I_{E1} = I_{E2} = I_{C3} = \frac{V_{EE} - \left[ \frac{R_2}{R_1 + R_2} V_{EE} \right] - V_{BE3}}{2R_E}$$

$$V_{B3} = \frac{R_2}{R_1 + R_2} (-V_{EE})$$

$$V_{E3} = V_{B3} - V_{BE3}$$

$$= -\frac{R_2}{R_1 + R_2} V_{EE} - V_{BE3}$$

$$I_{BE3} = I_{C3} = \frac{V_{E3} - (-V_{EE})}{R_E}$$

$$= \frac{V_{EE} - \left( \frac{R_2}{R_1 + R_2} \right) V_{EE} - V_{BE3}}{R_E}$$

The collector current I<sub>C3</sub> in transistor Q<sub>3</sub> is fixed and must be invariant signal is injected into either the emitter or the base of Q<sub>3</sub>. Thus the transistor Q<sub>3</sub> is a source of constant emitter current for transistor Q<sub>1</sub> and Q<sub>2</sub> of the differential amplifier.

### **CURRENT MIRROR CIRCUIT:**

The circuit in which the output current is forced to equal the input current is said to be a current mirror circuit. Thus in a current mirror circuit, the output current is a mirror image of the input current. Once the current I<sub>2</sub> is set up, the current I<sub>C3</sub> is automatically established to be nearly equal to I<sub>2</sub>. The current mirror is a special case of constant current bias and the current mirror bias requires of constant current bias and therefore can be used to set up currents in differential amplifier stages. The current mirror bias requires fewer components than constant current bias circuits. Since Q<sub>3</sub> and Q<sub>4</sub> are identical transistors the current and voltage are approximately same.

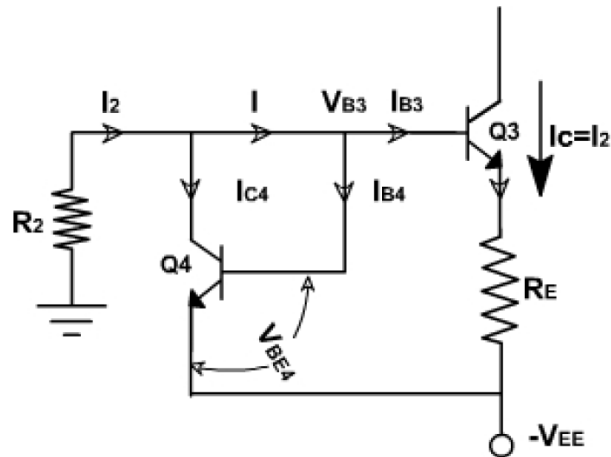


Fig 1.12 current mirror circuit

$$V_{BE3} = V_{BE4}$$

$$I_{B3} = I_{B4}$$

$$I_{C3} = I_{C4}$$

Summing currents at node  $V_{B3}$

$$I_2 = I_{C4} + I_{B3}$$

$$= I_{C4} + 2I_{B4} = I_{C3} + 2I_{B3}$$

$$= I_{C3} + 2 \left( \frac{I_{C3}}{\beta_{dc}} \right)$$

$$= I_{C3} \left( 1 + \frac{2}{\beta_{dc}} \right)$$

Generally  $\beta_{dc}$  is large enough, therefore  $\frac{2}{\beta_{dc}}$  is small.

$$\therefore I_2 \approx I_{C3}$$

$$I_2 = \frac{V_{EE} + V_{BE3}}{R_2}$$

## LEVEL TRANSLATOR:

Level shifting circuit is used to shift the dc level at the output downward to zero with respect to ground. An emitter follower with voltage divider is the simplest form of level translator. Instead of voltage divider emitter follower either with diode current bias or current mirror bias may be used to get better results. In this case, level shifter, which is common collector amplifier, shifts the level by 0.7V. If this shift is not sufficient, the output may be taken at the junction of two resistors in the emitter leg.